

Zadatak 10. Udaljenost žarišta hiperbole $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ jednaka je 20, a pravac $4x + 3y = 0$ je asimptota hiperbole. Nađi njezinu jednadžbu.

Rješenje.

$$2e = 20 = d(F_1, F_2) \implies e = 10$$

$$4x + 3y = 0 \text{ (asimptota)}$$

$$y = -\frac{4}{3}x \implies -\frac{b}{a} = -\frac{4}{3}, \quad b = \frac{4}{3}a$$

$$a^2 = e^2 - b^2$$

$$a^2 = e^2 - \left(\frac{4}{3}a\right)^2$$

$$\frac{25}{9}a^2 = e^2$$

$$\frac{25}{9}a^2 = 100 \quad / \cdot \frac{9}{25}$$

$$a^2 = 36 \implies a = 6$$

$$b = \frac{4}{3} \cdot 6 = 8 \implies b^2 = 64$$

$$H \quad \dots \quad \frac{x^2}{36} - \frac{y^2}{64} = 1$$