

Zadatak 13. Koliki kut zatvaraju asimptote hiperbole $3x^2 - y^2 = 9$?

Rješenje.

$$3x^2 - y^2 = 9 \quad / : 9$$

$$\frac{x^2}{3} - \frac{y^2}{9} = 1 \implies a = \sqrt{3}, \quad b = 3$$

asimptote ... $y = \pm \frac{b}{a}x$

$$y = \pm \frac{3}{\sqrt{3}}x$$

$$y = \pm \sqrt{3}x$$

$$\operatorname{tg} \alpha = \left| \frac{k_2 - k_1}{1 + k_1 k_2} \right| = \left| \frac{\sqrt{3} + \sqrt{3}}{1 - \sqrt{3}\sqrt{3}} \right| = \left| \frac{2\sqrt{3}}{1 - 3} \right| = \left| -\sqrt{3} \right| = \sqrt{3}$$

$$\implies \alpha = \frac{\pi}{3} = 60^\circ$$