

Zadatak 47. Odredi jednadžbu kružnice opisane trokutu kojem stranice leže na pravcima $2x + y + 1 = 0$, $x + 3y - 2 = 0$, $x - 7y + 38 = 0$.

Rješenje.

$$\begin{array}{r} x + 3y - 2 = 0 \\ x - 7y + 38 = 0 \\ \hline 10y - 40 = 0 \\ y = 4 \\ x = -10 \end{array}$$

$A(-10, 4)$

$$\begin{array}{r} 2x + y + 1 = 0 \\ x - 7y + 38 = 0 \\ \hline 14y - 76 + y + 1 = 0 \\ 15y = 75 \\ y = 5 \\ x = -3 \end{array}$$

$B(-3, 5)$

$$\begin{array}{r} 2x + y + 1 = 0 \\ x + 3y - 2 = 0 \\ \hline 4 - 6y + y + 1 = 0 \\ 5 - 5y = 0 \\ y = 1 \\ x = -1 \end{array}$$

$C(-1, 1)$

$$(-10 - p)^2 + (4 - q)^2 = r^2$$

$$(-3 - p)^2 + (5 - q)^2 = r^2$$

$$(-1 - p)^2 + (1 - q)^2 = r^2$$

$$100 + 20p + p^2 + 16 - 8q + q^2 = r^2$$

$$9 + 6p + p^2 + 25 - 10q + q^2 = r^2$$

$$1 + 2p + p^2 + 1 - 2q + q^2 = r^2$$

$$p^2 + q^2 + 20p - 8q + 116 = r^2$$

$$p^2 + q^2 + 6p - 10q + 34 = r^2$$

$$p^2 + q^2 + 2p - 2q + 2 = r^2$$

$$14p + 2q + 82 = 0$$

$$4p - 8q + 32 = 0$$

$$7p + q + 41 = 0$$

$$p - 2q + 8 = 0 \implies p = 2q - 8$$

$$14q - 56 + q + 41 = 0$$

$$15q = 15$$

$$q = 1$$

$$p = 2 - 8 = -6$$

$$36 + 1 - 12 - 2 + 2 = r^2$$

$$r^2 = 25$$

$$(x + 6)^2 + (y - 1)^2 = 25.$$