

■ Rješenja zadataka 6.2

Zadatak 1. Izračunaj duljinu treće stranice i ostala dva kuta trokuta ako je:

- 1) $a = 42$ cm, $b = 37.1$ cm, $\gamma = 67^\circ 19'$;
- 2) $a = 22.9$ cm, $c = 16.9$ cm, $\beta = 39^\circ 52'$;
- 3) $b = 3.8$ cm, $c = 5.2$ cm, $\alpha = 33^\circ 36'$;
- 4) $a = 13.2$ cm, $b = 5$ cm, $\gamma = 26^\circ 13'$;
- 5) $b = 1.55$ cm, $c = 2.15$ cm, $\alpha = 71^\circ 34'$.

Rješenje.

1)

$$a = 42\text{cm}$$

$$b = 37.1\text{cm}$$

$$\gamma = 67^\circ 19'$$

$$c, \alpha, \beta = ?$$

$$c^2 = a^2 + b^2 - 2ab \cos \gamma = 44\text{cm}^2$$

$$\cos \alpha = \frac{b^2 + c^2 - a^2}{2bc} = 0.474274$$

$$\alpha = 61^\circ 39'$$

$$\beta = 180^\circ - \alpha - \gamma = 51^\circ 2'$$

2)

$$a = 22.9\text{cm}$$

$$c = 16.9\text{cm}$$

$$\beta = 39^\circ 52'$$

$$b, \alpha, \gamma = ?$$

$$b^2 = a^2 + c^2 - 2ac \cos \beta = 14.7\text{cm}$$

$$\cos \alpha = \frac{b^2 + c^2 - a^2}{2bc} = -0.04570704021$$

$$\alpha = 92^\circ 40'$$

$$\gamma = 180^\circ - \alpha - \beta = 47^\circ 28'.$$

3)

$$b = 3.8\text{cm}$$

$$c = 5.2\text{cm}$$

$$\alpha = 33^\circ 36'$$

$$a, \beta, \gamma = ?$$

$$a^2 = b^2 + c^2 - 2bc \cos \alpha = 2.926\text{cm}$$

$$\cos \beta = \frac{a^2 + c^2 - b^2}{2ac} = 0.69540578$$

$$\beta = 45^\circ 57'$$

$$\gamma = 180^\circ - \alpha - \beta = 100^\circ 27'.$$

4)

$$a = 13.2\text{cm}$$

$$b = 5\text{cm}$$

$$\gamma = 26^\circ 13'$$

$$c, \alpha, \beta = ?$$

$$c^2 = a^2 + b^2 - 2ab \cos \gamma = 8.99\text{cm}$$

$$\cos \alpha = \frac{b^2 + c^2 - a^2}{2bc} = -0.76106674$$

$$\alpha = 139^\circ 34' 23''$$

$$\beta = 180^\circ - \alpha - \gamma = 14^\circ 13'.$$

5)

$$b = 1.55\text{cm}$$

$$c = 2.15\text{cm}$$

$$\alpha = 71^\circ 34'$$

$$a, \beta, \gamma = ?$$

$$a^2 = b^2 + c^2 - 2bc \cos \alpha = 2.22\text{cm}$$

$$\cos \beta = \frac{a^2 + c^2 - b^2}{2ac} = 0.74883721$$

$$\beta = 41^\circ 28' 53''$$

$$\gamma = 180^\circ - \alpha - \beta = 66^\circ 57' 7''.$$