

Zadatak 6. Zraka svjetlosti ima smjer određen pravcem $x - 2y + 5 = 0$. Odredi pravac na kojem je reflektirana zraka nakon odbijanja od pravca $3x - 2y + 7 = 0$.

Rješenje.

$$z \text{ (zraka)} \dots x - 2y + 5 = 0$$

$$p \text{ (pravac)} \dots \underline{3x - 2y + 7 = 0}$$

$$2y = x + 5$$

$$\underline{2y = 3x + 7}$$

$$y = \frac{1}{2}x + \frac{5}{2}$$

$$y = \frac{3}{2}x + \frac{7}{2}$$

$$\underline{\underline{\{T\}} = z \cap p}}$$

$$\frac{1}{2}x + \frac{5}{2} = \frac{3}{2}x + \frac{7}{2} \quad / \cdot 2$$

$$x + 5 = 3x + 7$$

$$2x = -2$$

$$x = -1$$

$$y = \frac{1}{2} \cdot (-1) + \frac{5}{2}$$

$$y = 2$$

$$\tg \varphi == \left| \frac{k_2 - k_1}{1 + k_1 k_2} \right| = \left| \frac{\frac{1}{2} - \frac{3}{2}}{1 + \frac{3}{2} \cdot \frac{1}{2}} \right| = \left| \frac{-1}{\frac{7}{4}} \right| = \frac{4}{7}$$

$$\varphi = \measuredangle(z, p) = \measuredangle(z', p)$$

$$\tg \varphi = \frac{4}{7} = \left| \frac{k_{z'} - k_1}{1 + k_1 k_{z'}} \right| = \left| \frac{k_{z'} - \frac{3}{2}}{1 + \frac{3}{2} \cdot k_{z'}} \right| = \left| \frac{\frac{2k_{z'} - 3}{2}}{\frac{2+3k_{z'}}{2}} \right| = \frac{|2k_{z'} - 3|}{|2 + 3k_{z'}|}$$

$$\frac{|2k_{z'} - 3|}{|2 + 3k_{z'}|} = \frac{4}{7}$$

$$7|2k_{z'} - 3| = 4|2 + 3k_{z'}|$$

$$2k_{z'} - 3 < 0 \implies k_{z'} < \frac{3}{2}$$

$$2 + 3k_{z'} < 0 \implies k_{z'} < -\frac{2}{3}$$

$$k_{z'} \in \left(-\frac{2}{3}, \frac{3}{2} \right)$$

$$k_{z'} \in \left(-\infty, -\frac{2}{3} \right) \cup \left(\frac{3}{2}, \infty \right)$$

$$-7(2k_{z'} - 3) = 4(2 + 3k_{z'})$$

$$-14k_{z'} + 21 = 8 + 12k_{z'}$$

$$26k_{z'} = 13$$

$$k_{z'} = \frac{1}{2} \text{ (koeficijent od } z\text{)}$$

$$7(2k_{z'} - 3) = 4(2 + 3k_{z'})$$

$$14k_{z'} - 21 = 8 + 12k_{z'}$$

$$2k_{z'} = 29$$

$$k_{z'} = \frac{29}{2}$$

z' prolazi točkom $T(-1, 2)$ i ima koeficijent smjera $k_{z'} = \frac{29}{2}$:

$$y - 2 = \frac{29}{2}(x + 1) \quad / \cdot 2$$

$$2y - 4 = 29x + 29$$

$$29x - 2y + 33 = 0$$