

Zadatak 11. Točkom $T(-2, 6)$ položi pravac koji s pravcima $5x - y + 4 = 0$ i $x + 5y - 6 = 0$ zatvara jednake kutove.

Rješenje.

$$T(-2, 6)$$

$$p \dots 5x - y + 4 = 0 \implies y = 5x + 4$$

$$q \dots x + 5y - 6 = 0 \implies y = -\frac{1}{5}x + \frac{6}{5}$$

$$r \dots y = kx + l, \quad T(-2, 6) \in r, \quad \measuredangle(p, r) = \measuredangle(q, r)$$

$$\operatorname{tg} \measuredangle(p, r) = \operatorname{tg} \measuredangle(q, r)$$

$$\left| \frac{k-5}{1+5k} \right| = \left| \frac{k+15}{1-\frac{1}{5}k} \right|$$

$$\left| \frac{k-5}{1+5k} \right| = \left| \frac{\frac{5k+1}{5}}{\frac{5-k}{5}} \right|$$

$$\left| \frac{k-5}{1+5k} \right| = \left| \frac{5k+1}{5-k} \right| \quad / \cdot |1+5k| \cdot |5-k|$$

$$|k-5| \cdot |5-k| = |5k+1| \cdot |1+5k|$$

$$\text{jer } |k-5| = |5-k|$$

$$|k-5|^2 = |5k+1|^2$$

$$(k-5)^2 = (5k+1)^2$$

$$k^2 - 10k + 25 = 25k^2 + 10k + 1$$

$$24k^2 + 20k - 24 = 0 \quad / : 4$$

$$6k^2 + 5k - 6 = 0$$

$$k_{1,2} = \frac{-5 \pm \sqrt{25 + 144}}{12} = \frac{-5 \pm 13}{12}$$

$$k_1 = -\frac{3}{2}, \quad k_2 = \frac{2}{3}$$

$$T(-2, 6), \quad k_1 = -\frac{3}{2}$$

$$T(-2, 6), \quad k_2 = \frac{2}{3}$$

$$y - 6 = -\frac{3}{2}(x + 2) \quad / \cdot 2$$

$$y - 6 = \frac{2}{3}(x + 2) \quad / \cdot 3$$

$$2y - 12 = -3x - 6$$

$$3y - 18 = 2x + 4$$

$$3x + 2y - 6 = 0$$

$$2x - 3y + 22 = 0$$