

Zadatak 12. Kako glasi jednačba pravca koji prolazi točkom $T(2, 1)$ i s pravcem $2x + 3y + 4 = 0$ zatvara kut od 45° ?

Rješenje.

$$T(2, 1)$$

$$p \dots 2x + 3y + 4 = 0 \implies y = -\frac{2}{3}x - \frac{4}{3}$$

$$r \dots y = kx + l$$

$$\varphi = 45^\circ \implies \operatorname{tg} \varphi = 1$$

$$\operatorname{tg} \varphi = 1$$

$$\left| \frac{k + \frac{2}{3}}{1 - \frac{2}{3}k} \right| = 1$$

$$\left| \frac{\frac{3k+2}{3}}{\frac{3-2k}{3}} \right| = 1$$

$$\left| \frac{3k+2}{3-2k} \right| = 1 \quad / \cdot |3-2k|$$

$$|3k+2| = |3-2k|$$

$$3k+2 < 0 \implies k < -\frac{2}{3}$$

$$3-2k < 0 \implies k > \frac{3}{2}$$

	$\langle -\infty, -\frac{2}{3} \rangle$	$\langle -\frac{2}{3}, \frac{3}{2} \rangle$	$\langle \frac{3}{2}, \infty \rangle$
$3k+2$	-	+	+
$3-2k$	+	+	-

$$\langle -\infty, -\frac{2}{3} \rangle \cup \langle \frac{3}{2}, \infty \rangle$$

$$3-2k = -3k-2$$

$$k = -5$$

$$y-1 = -5(x-2)$$

$$y-1 = -5x+10$$

$$5x - y - 11 = 0$$

$$\langle -\frac{2}{3}, \frac{3}{2} \rangle$$

$$3-2k = 3k+2$$

$$k = \frac{1}{5}$$

$$y-1 = \frac{1}{5}x - \frac{2}{5} \quad / \cdot 5$$

$$5y-5 = x-2$$

$$x-5y+3=0$$