

Zadatak 15. Ako je $\cos\left(\frac{\pi}{4} + x\right) = -\frac{\sqrt{2}}{3}$, $\pi < x < \frac{3\pi}{2}$, izračunaj $\cos x$.

Rješenje. $\pi < x < \frac{3\pi}{2} \implies \sin x, \cos x < 0, \sin\left(\frac{\pi}{4} + x\right) < 0$

$$\sin\left(\frac{\pi}{4} + x\right) = -\sqrt{1 - \sin^2\left(\frac{\pi}{4} + x\right)} = -\sqrt{1 - \frac{2}{9}} = -\frac{\sqrt{7}}{3}$$

$$\cos\left(\frac{\pi}{4} + x\right) = \cos\frac{\pi}{4}\cos x - \sin\frac{\pi}{4}\sin x = -\frac{\sqrt{2}}{3}$$

$$\sin\left(\frac{\pi}{4} + x\right) = \sin\frac{\pi}{4}\cos x + \cos\frac{\pi}{4}\sin x = -\frac{\sqrt{7}}{3}$$

$$\left. \begin{array}{l} \frac{\sqrt{2}}{2}\cos x - \frac{\sqrt{2}}{2}\sin x = -\frac{\sqrt{2}}{3} \\ \frac{\sqrt{2}}{2}\cos x + \frac{\sqrt{2}}{2}\sin x = -\frac{\sqrt{7}}{3} \end{array} \right\} +$$

$$\sqrt{2}\cos x = \frac{-\sqrt{2} - \sqrt{7}}{3} \quad / : \sqrt{2}$$

$$\cos x = \frac{-\sqrt{2} - \sqrt{7}}{3\sqrt{2}} = -\frac{\sqrt{2} + \sqrt{7}}{3\sqrt{2}}$$