

Zadatak 24. Ako je $\cos \alpha = 0.6$, $\frac{3\pi}{2} < \alpha < 2\pi$, $\sin \beta = -\frac{40}{41}$, $\pi < \beta < \frac{3\pi}{2}$, koliko je $\operatorname{ctg}(\alpha - \beta)$?

Rješenje. $\frac{3\pi}{2} < \alpha < 2\pi$, $\pi < \beta < \frac{3\pi}{2}$;

$$\sin \alpha = -\sqrt{1 - \cos^2 \alpha} = -\sqrt{1 - 0.36} = -\sqrt{0.64} = -0.8$$

$$\cos \beta = -\sqrt{1 - \sin^2 \beta} = -\sqrt{1 - \frac{1600}{1681}} = -\sqrt{\frac{81}{1681}} = -\frac{9}{41}$$

$$\operatorname{ctg} \alpha = \frac{\cos \alpha}{\sin \alpha} = \frac{0.6}{-0.8} = -\frac{6}{8} = -\frac{3}{4}$$

$$\operatorname{ctg} \beta = \frac{\cos \beta}{\sin \beta} = \frac{-\frac{9}{41}}{-\frac{40}{41}} = \frac{9}{41}$$

$$\operatorname{ctg}(\alpha - \beta) = \frac{\operatorname{ctg} \alpha \cdot \operatorname{ctg} \beta + 1}{\operatorname{ctg} \beta - \operatorname{ctg} \alpha} = \frac{-\frac{3}{4} \cdot \frac{9}{41} + 1}{\frac{9}{41} - \left(-\frac{3}{4}\right)} = \frac{\frac{133}{160}}{\frac{39}{40}} = \frac{133}{156}$$