

Zadatak 29. Ako je $\alpha + \beta = \frac{3\pi}{4}$, koliko je $(1 + \operatorname{ctg} \alpha)(1 + \operatorname{ctg} \beta)$?

Rješenje. $\alpha + \beta = \frac{3\pi}{4}$;

$$\operatorname{ctg}(\alpha + \beta) = \frac{\operatorname{ctg} \alpha \cdot \operatorname{ctg} \beta - 1}{\operatorname{ctg} \alpha + \operatorname{ctg} \beta} = \operatorname{ctg} \frac{3\pi}{4} = -1$$

$$\implies \operatorname{ctg} \alpha + \operatorname{ctg} \beta = 1 - \operatorname{ctg} \alpha \cdot \operatorname{ctg} \beta$$

$$(1 + \operatorname{ctg} \alpha)(1 + \operatorname{ctg} \beta) = 1 + \underbrace{\operatorname{ctg} \alpha + \operatorname{ctg} \beta}_{1 - \operatorname{ctg} \alpha \cdot \operatorname{ctg} \beta} + \operatorname{ctg} \alpha \cdot \operatorname{ctg} \beta =$$

$$1 + 1 - \operatorname{ctg} \alpha \cdot \operatorname{ctg} \beta + \operatorname{ctg} \alpha \cdot \operatorname{ctg} \beta = 2$$