

Zadatak 33. Koliko je $\cos(a - b)$ ako je $\sin a + \sin b = 1$, $\cos a + \cos b = \sqrt{2}$?

Rješenje.

$$\begin{aligned}\sin a + \sin b &= 1 \quad /^2 \\ \cos a + \cos b &= \sqrt{2} \quad /^2\end{aligned}$$

$$\left. \begin{aligned}\sin^2 a + 2 \sin a \cdot \sin b + \sin^2 b &= 1 \\ \cos^2 a + 2 \cos a \cdot \cos b + \cos^2 b &= 2\end{aligned} \right\} +$$

$$1 + 2 \sin a \cdot \sin b + 2 \cos a \cdot \cos b + 1 = 3$$

$$2(\sin a \cdot \sin b + \cos a \cdot \cos b) = 3 - 2$$

$$2 \cos(a - b) = 1$$

$$\cos(a - b) = \frac{1}{2}$$

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