

Zadatak 16. Izračunaj vrijednost razlomka $\frac{2 \sin 2\alpha + \sin 4\alpha}{2 \sin 2\alpha - \sin 4\alpha}$ ako je $\cos \alpha = -\frac{1}{2}$.

Rješenje.

$$\begin{aligned} \frac{2 \sin 2\alpha + \sin 4\alpha}{2 \sin 2\alpha - \sin 4\alpha} &= \frac{2 \sin 2\alpha + 2 \sin 2\alpha \cos 2\alpha}{2 \sin 2\alpha - 2 \sin 2\alpha \cos 2\alpha} = \frac{2 \sin 2\alpha(1 + \cos 2\alpha)}{2 \sin 2\alpha(1 - \cos 2\alpha)} \\ &= \frac{1 + \cos^2 \alpha - \sin^2 \alpha}{1 - \cos^2 \alpha + \sin^2 \alpha} = \frac{2 \cos^2 \alpha}{2 \sin^2 \alpha} = \frac{\cos^2 \alpha}{1 - \cos^2 \alpha} = \frac{\frac{1}{4}}{1 - \frac{1}{4}} = \frac{1}{3} \end{aligned}$$