

Zadatak 9. Dokaži: $\cos 36^\circ - \cos 72^\circ = \frac{1}{2}$.

Rješenje.

$$\cos 36^\circ - \cos 72^\circ = \frac{1}{2}$$

$$-2 \sin \frac{36^\circ + 72^\circ}{2} \sin \frac{36^\circ - 72^\circ}{2} = \frac{1}{2}$$

$$-2 \sin 54^\circ \sin(-18^\circ) = \frac{1}{2}$$

$$2 \sin 54^\circ \sin 18^\circ = \frac{1}{2}$$

$$2 \cos(90^\circ - 54^\circ) \sin 18^\circ = \frac{1}{2}$$

$$2 \cos 36^\circ \sin 18^\circ = \frac{1}{2}$$

$$\frac{2 \cos 36^\circ \sin 18^\circ \cos 18^\circ}{\cos 18^\circ} = \frac{1}{2}$$

$$\frac{\cos 36^\circ \sin 36^\circ}{\cos 18^\circ} = \frac{1}{2}$$

$$\frac{\frac{1}{2} \sin 72^\circ}{\cos 18^\circ} = \frac{1}{2}$$

$$\frac{\frac{1}{2} \cos(90^\circ - 72^\circ)}{\cos 18^\circ} = \frac{1}{2}$$

$$\frac{1}{2} = \frac{1}{2}$$