

Zadatak 6. Točke $B(1, -2)$ i $C(3, 2)$ vrhovi su paralelograma $ABCD$, a točka $S\left(-\frac{1}{2}, \frac{3}{2}\right)$ sjecište je njegovih dijagonala. Odredi vrhove A i D ovog paralelograma.

Rješenje.

$$A(x_A, y_A),$$

$$B(1, -2),$$

$$S\left(-\frac{1}{2}, \frac{3}{2}\right),$$

$$C(3, 2),$$

$$D(x_D, y_D),$$

$$A, D = ?$$

$$\overrightarrow{AS} = \overrightarrow{SC}$$

$$\left(-\frac{1}{2} - x_A\right)\vec{i} + \left(\frac{3}{2} - y_A\right)\vec{j} = \left(3 + \frac{1}{2}\right)\vec{i} + \left(2 - \frac{3}{2}\right)\vec{j}$$

$$\left(-\frac{1}{2} - x_A\right)\vec{i} + \left(\frac{3}{2} - y_A\right)\vec{j} = \frac{7}{2}\vec{i} + \frac{1}{2}\vec{j}$$

$$-\frac{1}{2} - x_A = \frac{7}{2} \implies x_A = -4$$

$$\frac{3}{2} - y_A = \frac{1}{2} \implies y_A = 1$$

$$\implies A(-4, 1)$$

$$\overrightarrow{BS} = \overrightarrow{SD}$$

$$\left(-\frac{1}{2} - 1\right)\vec{i} + \left(\frac{3}{2} + 2\right)\vec{j} = \left(x_D + \frac{1}{2}\right)\vec{i} + \left(y_D - \frac{3}{2}\right)\vec{j}$$

$$-\frac{3}{2}\vec{i} + \frac{7}{2}\vec{j} = \left(x_D + \frac{1}{2}\right)\vec{i} + \left(y_D - \frac{3}{2}\right)\vec{j}$$

$$-\frac{3}{2} = x_D + \frac{1}{2} \implies x_D = -2$$

$$\frac{7}{2} = y_D - \frac{3}{2} \implies y_D = 5$$

$$\implies D(-2, 5)$$