

Zadatak 9. Točke $A(-2, 1)$, $B(3, 0)$, $C(2, 5)$, $D(-3, 6)$ su vrhovi romba. Dokaži!

Rješenje.

$$\overrightarrow{AB} = \overrightarrow{DC} \quad (1)$$

$$\overrightarrow{AD} = \overrightarrow{BC} \quad (2),$$

$$|\overrightarrow{AB}| = |\overrightarrow{DC}| = |\overrightarrow{AD}| = |\overrightarrow{BC}| \quad (3)$$

$$(1) \begin{cases} \overrightarrow{AB} = (3 + 2)\vec{i} + (0 - 1)\vec{j} = 5\vec{i} - \vec{j} \\ \overrightarrow{DC} = (2 + 3)\vec{i} + (5 - 6)\vec{j} = 5\vec{i} - \vec{j} \end{cases}$$

$$(2) \begin{cases} \overrightarrow{AD} = (-3 + 2)\vec{i} + (6 - 1)\vec{j} = -\vec{i} + 5\vec{j} \\ \overrightarrow{BC} = (2 - 3)\vec{i} + (5 - 0)\vec{j} = -\vec{i} + 5\vec{j} \end{cases}$$

$$(3) \begin{cases} |\overrightarrow{AB}| = \sqrt{5^2 + (-1)^2} = \sqrt{26} = |\overrightarrow{DC}| \\ |\overrightarrow{AD}| = \sqrt{(-1)^2 + 5^2} = \sqrt{26} = |\overrightarrow{BC}| \end{cases}$$