

**Zadatak 5.** Odredi vektor  $\vec{b}$  kolinearan s vektorom  $\vec{a} = \vec{i} - 2\vec{j}$  ako je  $\vec{a} \cdot \vec{b} = -15$ .

**Rješenje.**  $\vec{b}$  kolinearan s  $\vec{a} \implies \vec{b} \parallel \vec{a} \implies \sphericalangle(\vec{a}, \vec{b}) = 180^\circ$ .

$$\vec{b} = b_x \vec{i} + b_y \vec{j}$$

$$\begin{aligned} \vec{a} \cdot \vec{b} &= a_x b_x + a_y b_y \\ &= 1 \cdot b_x + (-2)b_y \end{aligned}$$

$$b_x - 2b_y = -15$$

$$b_x = 2b_y - 15$$

$$|\vec{a}| = \sqrt{1+4} = \sqrt{5}, \quad \vec{b} = \lambda \vec{a}$$

$$\cos \sphericalangle(\vec{a}, \vec{b}) = -1 = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}| \cdot |\vec{b}|}$$

$$-1 = \frac{-15}{\sqrt{5} \cdot |\lambda| \sqrt{5}}$$

$$-1 = \frac{-15}{5|\lambda|} / \cdot 5|\lambda|$$

$$-5|\lambda| = -15$$

$$|\lambda| = 3$$

$$\implies \lambda = -3 \text{ jer je } \sphericalangle(\vec{a}, \vec{b}) = 180^\circ.$$

$$\vec{b} = -3(\vec{i} - 2\vec{j}) = -3\vec{i} + 6\vec{j}.$$