

Zadatak 3. Skrati razlomke:

1) $\frac{15!}{13!};$

2) $\frac{8!}{5!};$

3) $\frac{n!}{(n-2)!};$

4) $\frac{(n+1)!}{(n-1)!};$

5) $\frac{(2n)!}{n!};$

6) $\frac{(n+k)!}{(n+k-2)!};$

7) $\frac{(n+1)!}{(n-2)!};$

8) $\frac{2n(2n-1)}{(2n)!}.$

Rješenje.

1) $\frac{15!}{13!} = \frac{13! \cdot 14 \cdot 15}{13!} = 14 \cdot 15 = 210;$

2) $\frac{8!}{5!} = \frac{5! \cdot 6 \cdot 7 \cdot 8}{5!} = 6 \cdot 7 \cdot 8 = 336;$

3) $\frac{n!}{(n-2)!} = \frac{(n-2)!(n-1)n}{(n-2)!} = (n-1)n;$

4) $\frac{(n+1)!}{(n-1)!} = \frac{(n-1)!n(n+1)}{(n-1)!} = n(n+1);$

5) $\frac{(2n)!}{n!} = \frac{n!(n+1)(n+2) \cdots (2n)}{n!} = (n+1)(n+2) \cdots (2n);$

6) $\frac{(n+k)!}{(n+k-2)!} = \frac{(n+k-2)!(n-k-1)(n-k)}{(n+k-2)!} = (n-k-1)(n-k);$

7) $\frac{(n+1)!}{(n-2)!} = \frac{(n-2)!(n-1)n(n+1)}{(n-2)!} = (n-1)n(n+1);$

8) $\frac{2n(2n-1)}{(2n)!} = \frac{2n(2n-1)}{(2n-2)!(2n-1)(2n)} = \frac{1}{(2n-2)!}.$