

Zadatak 4.

Napiši jednadžbu tangente na krivulju

$$y = \cos\left(2x - \frac{\pi}{3}\right) + 2 \text{ u točki s apscisom } x_0 = \frac{\pi}{2}.$$

Rješenje. $y\left(\frac{\pi}{2}\right) = \cos\left(\pi - \frac{\pi}{3}\right) + 2 = \cos\frac{2\pi}{3} + 2 = -\frac{1}{2} + 2 = \frac{3}{2}; y' = -2 \sin\left(2x - \frac{\pi}{3}\right) \implies y'\left(\frac{\pi}{2}\right) = -2 \sin\left(\frac{2\pi}{2} - \frac{\pi}{3}\right) = -2 \sin\frac{2\pi}{3} = -\sqrt{3}.$ Jednadžba tangente glasi $y - \frac{3}{2} = -\sqrt{3}\left(x - \frac{\pi}{2}\right),$ odnosno $y = -\sqrt{3}x + \frac{1}{2}(\pi\sqrt{3} + 3).$