

Zadatak 35.

Riješi jednadžbu $(g \circ f)(x) = 4$ ako je

$$f(x) = \log_{0.25} \frac{1}{x^2 - x + 4}, \quad g(x) = 2^{x+1}.$$

Rješenje.

$$f(x) = \log_{0.25} \frac{1}{x^2 - x + 4} = \log_4(x^2 - x + 4), \quad g(x) = 2^{x+1}$$

$$(g \circ f)(x) = 2^{\log_4(x^2 - x + 4) + 1} = 2^{\frac{1}{2} \log_2(x^2 - x + 4) + \log_2 2}$$
$$= 2^{\log_2 2\sqrt{x^2 - x + 4}} = 2\sqrt{x^2 - x + 4}$$

$$2\sqrt{x^2 - x + 4} = 4 \implies \sqrt{x^2 - x + 4} = 2 \quad |^2 \implies x^2 - x + 4 = 4$$
$$\implies x(x - 1) = 0 \implies x_1 = 0, x_2 = 1.$$