

Zadatak 14. U skupu \mathbf{R} riješi jednadžbu $\int_x^{x+1} (t^3 + 4) dt = \frac{11}{4}$.

Rješenje.

$$\begin{aligned}\int_x^{x+1} (t^3 + 4) dt &= \int_x^{x+1} t^3 dt + 4 \int_x^{x+1} dt = \frac{t^4}{4} \Big|_x^{x+1} + 4t \Big|_x^{x+1} = \frac{1}{4}[(x+1)^4 - \\ &\quad x^4] + 4(x+1 - x) = \frac{1}{4}(x^4 + 4x^3 + 4x^2 + 2x^2 + 4x + 1 - x^4) + 4 = \\ &= \frac{1}{4}(4x^3 + 6x^2 + 4x + 1) + 4 = x^3 + \frac{3}{2}x^2 + x + \frac{17}{4}. \\ x^3 + \frac{3}{2}x^2 + x + \frac{17}{4} &= \frac{11}{4} \\ x^3 + \frac{3}{2}x^2 + x + \frac{3}{2} &= 0 \\ x(x^2 + 1) + \frac{3}{2}(x^2 + 1) &= 0 \\ \left(x + \frac{3}{2}\right)(x^2 + 1) &= 0 \\ x &= -\frac{3}{2}\end{aligned}$$