

Zadatak 26. Nađi površinu lika omeđenog krivuljama $y = 6x^2 - 5x + 1$, $y = \cos \pi x$ i pravcima $x = 0$, $x = 1$.

Rješenje.

$$\begin{aligned}
 P &= \int_0^{\frac{1}{2}} (\cos \pi x - 6x^2 + 5x - 1) dx + \int_{\frac{1}{2}}^1 (6x^2 - 5x + 1 - \cos \pi x) dx = \\
 &\quad \left. \frac{\sin \pi x}{\pi} \right|_0^{\frac{1}{2}} - \left. \frac{6x^3}{3} \right|_0^{\frac{1}{2}} + \left. \frac{5x^2}{2} \right|_0^{\frac{1}{2}} - \left. x \right|_0^{\frac{1}{2}} + \left. \frac{6x^3}{3} \right|_{\frac{1}{2}}^1 - \left. \frac{5x^2}{2} \right|_{\frac{1}{2}}^1 + \left. x \right|_{\frac{1}{2}}^1 - \left. \frac{\sin \pi x}{\pi} \right|_{\frac{1}{2}}^1 = \frac{1}{\pi} \left(\sin \frac{\pi}{2} - \sin 0 \right) - 2 \cdot \frac{1}{8} + \frac{5}{2} \cdot \frac{1}{4} - \frac{1}{2} + 2 \left(1 - \frac{1}{8} \right) - \frac{5}{2} \left(1 - \frac{1}{4} \right) - \frac{1}{\pi} \left(\sin \pi - \sin \frac{\pi}{2} \right) = \\
 &\quad \pi - \frac{1}{4} + \frac{5}{8} - \frac{1}{2} + \frac{14}{8} - \frac{15}{16} + \frac{1}{\pi} = \frac{\pi}{\pi} - \frac{1}{4}.
 \end{aligned}$$

